

Bring — calculator

* tablet w/pen — plug in

pencil & paper

QR textbook

↳ Using & Understanding Mathematics

Assignment zero — hello videos

PA#0 — exponents

PA#1 — Summation Notation

Assignment: super detailed work

You must
Show Work
to receive
any credit

$\frac{a^6}{a^3}$ ~~$= a^3$~~

$(a^3)^2$ ~~$= a^6$~~

$a^{6-3} = a^{6+(-3)} = a^3$

$= a^{(3)(2)} = a^{3 \cdot 2} = a^6$

OK in future

Summation Notation

$$\sum_{i=3}^6 i^2 \Rightarrow i^2 + i^2 + i^2 + i^2 + i^2$$

$$\sum_{k=0}^6 k! = k! + k! + k! + k!$$

\sum ← "sum"

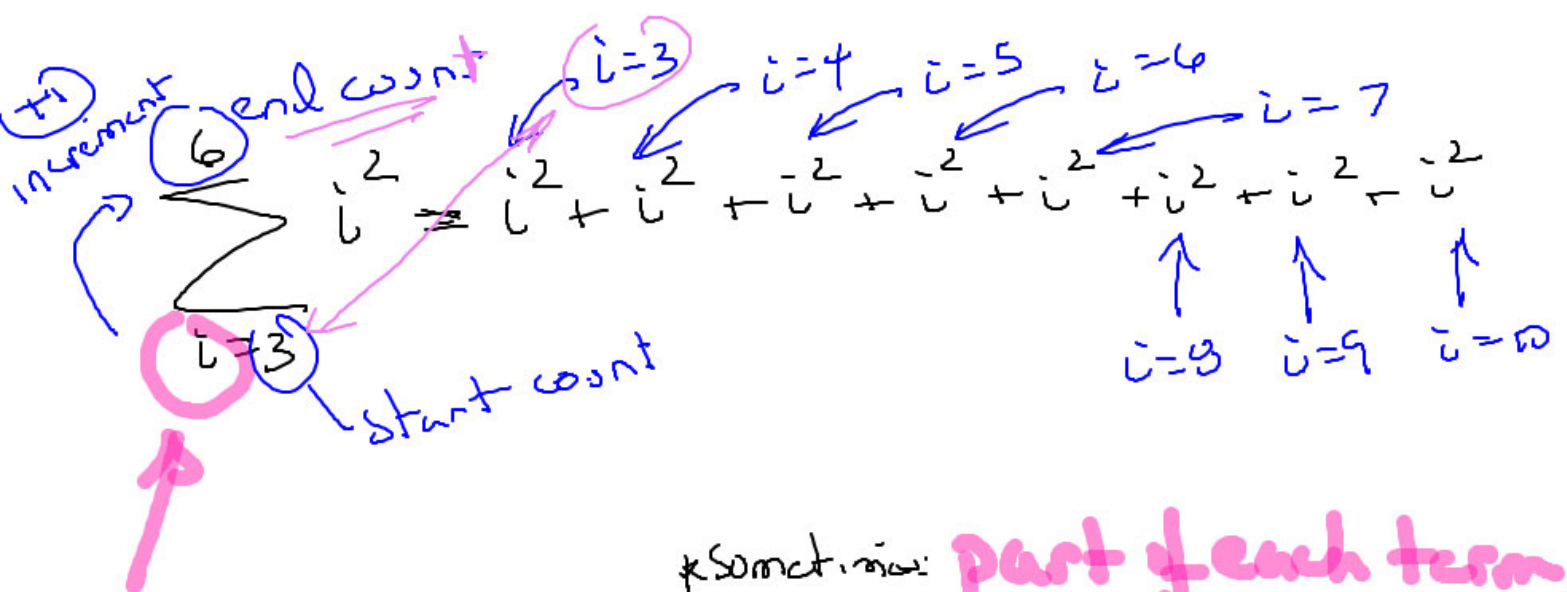
↑
Capital Greek
letters

Sums whatever is
to the right of \sum

$$\sum \square = \square + \square + \square$$

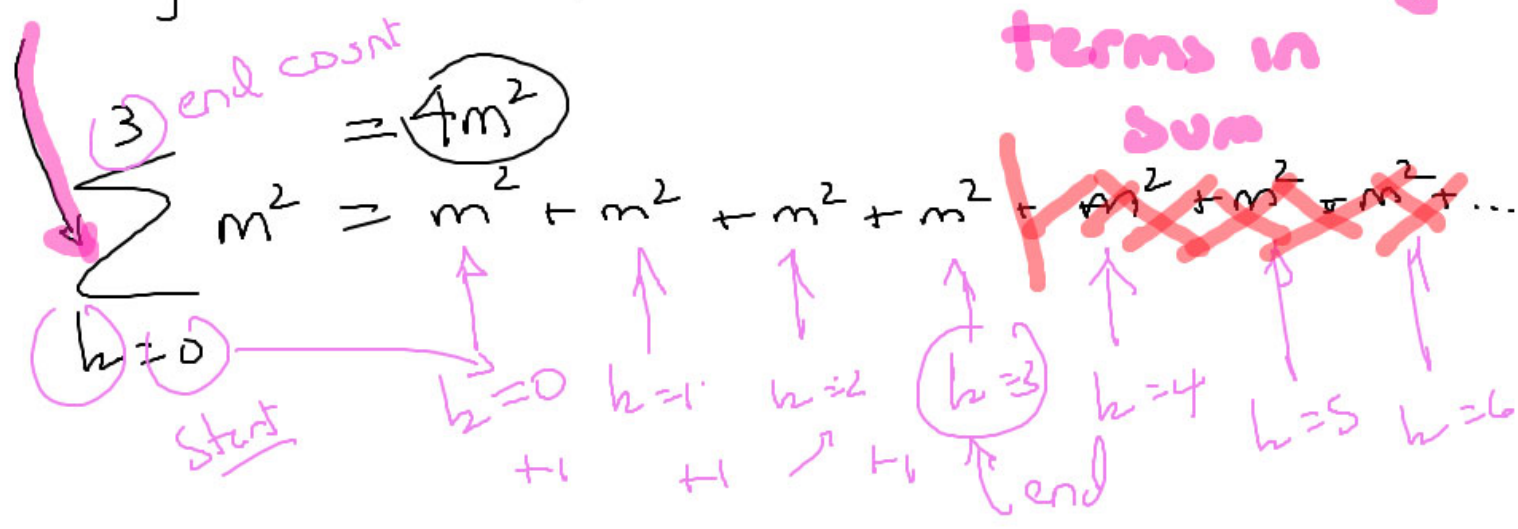
SUM

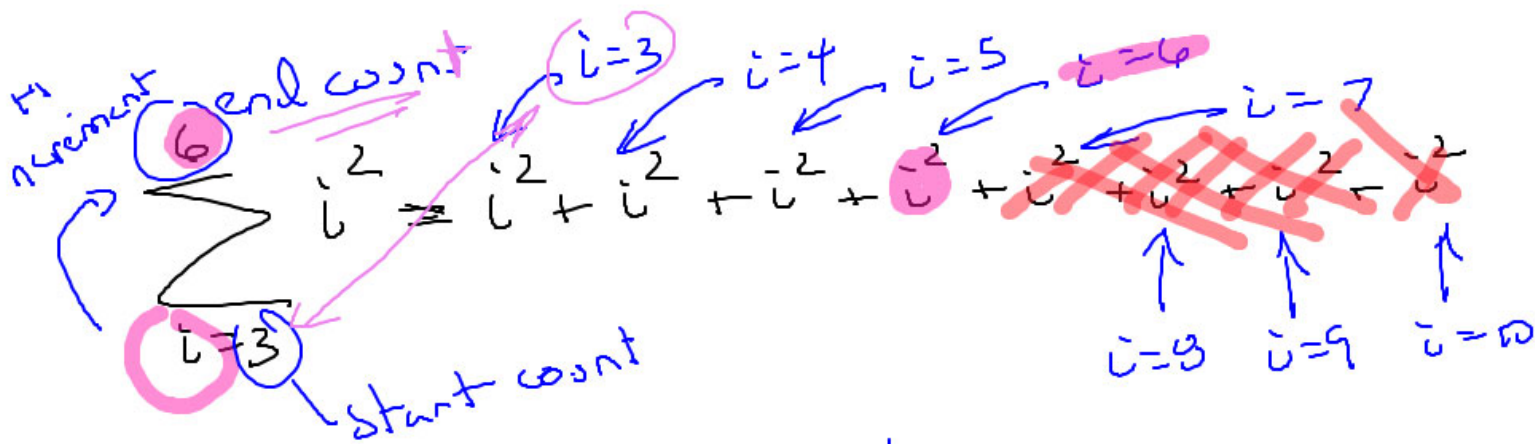
$$\sum \frac{6j^2}{(m-3)} = \frac{6j^2}{(m-3)} + \frac{6j^2}{(m-3)} + \frac{6j^2}{(m-3)} + \dots$$



Index of summation \rightarrow **COUNTER** — how many terms in sum

**Sometimes: part of each term*





$$\begin{aligned}
 &= \cancel{3^2} + \cancel{4^2} + \cancel{5^2} + 6^2 = 3^2 + 4^2 + 5^2 + 6^2 \\
 &= 9 + 16 + 25 + 36 \\
 &= \underline{\underline{86}}
 \end{aligned}$$

$$\sum_{i=3}^6 i^2 = 86$$

$$\sum_{h=1}^3 \frac{3h!}{(5-h)^2} = \frac{3 \cdot 1!}{(5-1)^2} + \frac{3 \cdot 2!}{(5-2)^2} + \frac{3 \cdot 3!}{(5-3)^2}$$

Counter evaluates terms using $h=1$

$h=1$ $h=2$ $h=3$

$$= \frac{3(1)!}{(5-1)^2} + \frac{3(2)!}{(5-2)^2} + \frac{3(3)!}{(5-3)^2}$$

$$= \frac{3(1)}{16} + \frac{3(2)}{9} + \frac{3(6)}{4} = \frac{3}{16} + \frac{6}{9} + \frac{18}{4}$$

$$= \frac{3(1)}{16} + \frac{3(2)}{9} + \frac{3(6)}{4} = \frac{3}{16} + \frac{6}{9} + \frac{18}{4}$$

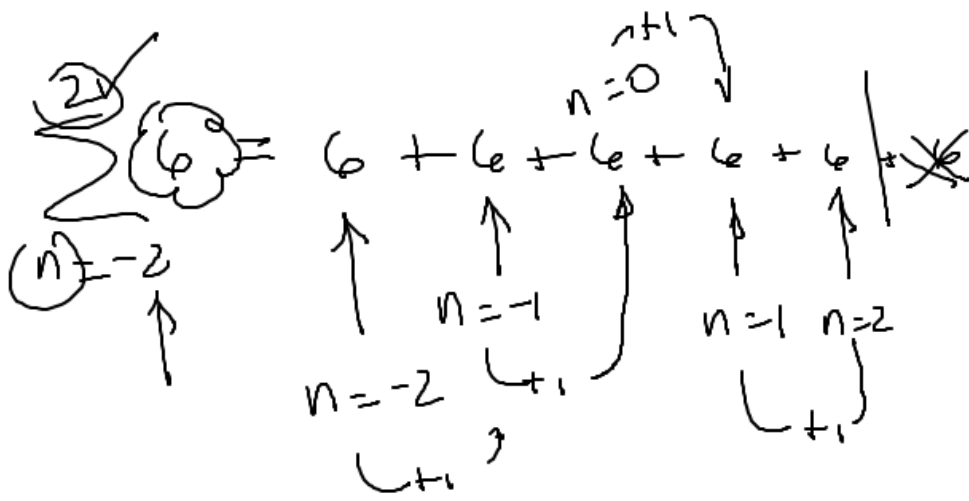
$$(\underline{16 \times 9 = 144} \quad 144/4 = 36)$$

$$= \frac{3}{16} \left(\frac{9}{9} \right) + \frac{6}{9} \left(\frac{16}{16} \right) + \frac{18}{4} \left(\frac{36}{36} \right)$$

$$= \frac{27}{144} + \frac{96}{144} + \frac{648}{144} = \frac{771}{144} = \frac{257}{48}$$

$$= \underline{5,3541\bar{6}} \checkmark$$

better \nearrow



$$= 6 + 6 + 6 + 6 + 6 = 30$$

$$\sum_{n=-2}^2 6 = 30$$

Stop value of k

$$\sum_{k=-2}^1 \frac{k^2}{k-3} = \frac{1^2}{1-3} + \frac{(-1)^2}{(-1-3)} + \frac{0^2}{0-3} + \frac{1^2}{1-3}$$

\uparrow \uparrow \uparrow \uparrow
 $k = -2$ $k = -1$ $k = 0$ $k = 1$

index of summation is always an integer

- ✓ k - counter
- ✓ use k to evaluate each term

$$= \frac{(-2)^2}{(-2-3)} + \frac{(-1)^2}{(-1-3)} + \frac{0^2}{(0-3)} + \frac{1^2}{(1-3)}$$

$$= \frac{(-2)^2}{(-2-3)} + \frac{(-1)^2}{(-1-3)} + \frac{0^2}{(0-3)} + \frac{1^2}{(1-3)}$$

$$= \frac{4}{-5} + \frac{1}{-4} + \frac{0}{-3} + \frac{1}{-2}$$

$$= -\frac{4}{5} - \frac{1}{4} + 0 - \frac{1}{2}$$

$$= -\frac{16}{20} - \frac{5}{20} + 0 - \frac{10}{20} = \underline{\underline{\underline{-\frac{31}{20}}}}$$

$$\sum_{m=-2}^2 \frac{|m|^2}{(3-m)^2} =$$

index of summation

$$\sum_{j=1}^3 \frac{6^2}{3} = \sum_{j=1}^3 \frac{6^2}{3} + \sum_{j=2}^3 \frac{6^2}{3} + \sum_{j=3}^3 \frac{6^2}{3} = 3 \left(\frac{6^2}{3} \right) = \frac{3(36)}{3}$$

$$= \frac{108}{3} = 36$$

$$\sum_{m=-2}^2 \frac{|m|^2}{(3-m)^2} = \frac{|m|^2}{(3-m)^2} \Big|_{m=-2} + \frac{|m|^2}{(3-m)^2} \Big|_{m=-1} + \frac{|m|^2}{(3-m)^2} \Big|_{m=0} + \frac{|m|^2}{(3-m)^2} \Big|_{m=1} + \frac{|m|^2}{(3-m)^2} \Big|_{m=2}$$

$$= \frac{(-2)^2}{[3-(-2)]^2} + \frac{(-1)^2}{[3-(-1)]^2} + \frac{(0)^2}{(3-0)^2} + \frac{(1)^2}{(3-1)^2} + \frac{(2)^2}{(3-2)^2}$$

$$= \frac{4}{25} + \frac{1}{16} + 0 + \frac{1}{4} + \frac{4}{1} =$$

$$= \frac{32}{400} + \frac{25}{400} + 0 + \frac{100}{400} + \frac{1600}{400} = \frac{1759}{400}$$